



**BC COMS 1016:  
Intro to Comp Thinking & Data Science**

**—  
Lecture 26 —  
Final Project Discussion  
Review**

**—  
Jupyter on your Computer  
Q&A**

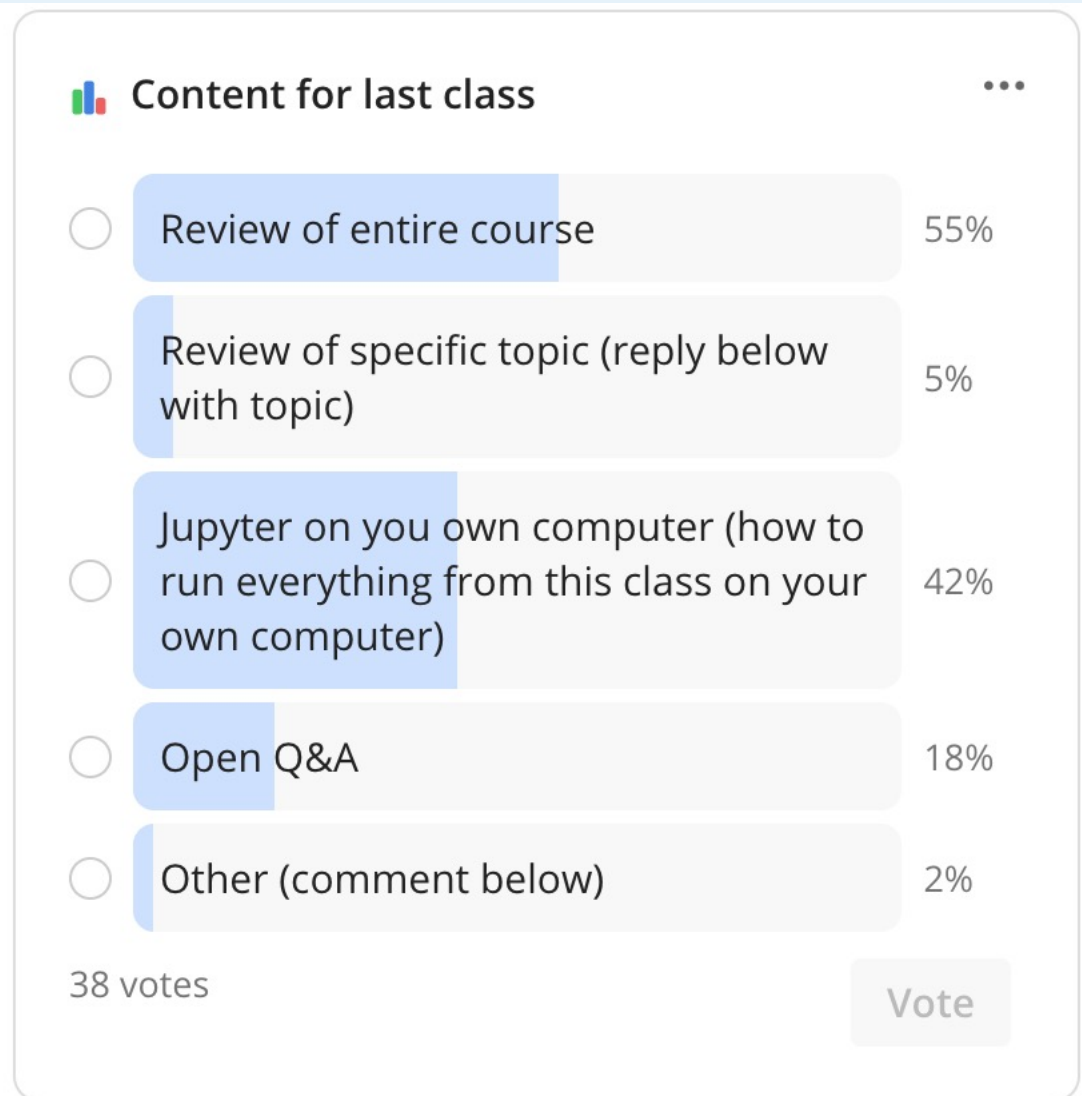


- Homework 10 – Classification
  - Due Monday 05/04
  
- Course Evaluations:
  - Due XXX
  
- Project 3:
  - Due Monday 05/04

# Outline for Today's Class



- Course Project
- Review
- Jupyter on your computer
- Q&A





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# Final Project

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- Explore a real world dataset from multiple tables
  - Choose from 6 datasets
- Ask 2 questions that the dataset can help answer
  - Hypothesis Testing
  - Prediction
- Use methods covered in in the class to answer these questions

# 6 Datasets to choose from



US-wealth



airbnb



contraceptive-data



example



fma-analysis



hr-dataset



police-scorecard



We will provide:

1. An overview and description of the dataset
2. A preview section with code to read in all the datasets relevant to your specific project
3. A Research Report section which contains the outline for the content of your final project.



1. Introduction:  
250-300 word background
2. Hypothesis Testing and Prediction Questions  
State the questions and how you plan to answer them
3. Exploratory Data Analysis
  1. Visualize!
4. Hypothesis Testing
5. Prediction
6. Conclusion





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## 2. Hypothesis Testing and Prediction Questions

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## 3. Exploratory Data Analysis

1. Visualize!

## 4. Hypothesis Testing

## 5. Prediction

## 6. Conclusion

The earlier you submit the proposal the better so we can give you more feedback



## Randomization

**Question: How do we make our random simulations reproducible?**

**Answer: `random.np.seed()`, `random.seed()`**



# Classifiers Evaluation



- Split data into training and test splits
- Question: Why?
- Answer: To see how well our classifier generalizes to unseed data



- Scenario: Classifier to predict if a student will pass or fail, binary classification
- Question: What should our features be?
  - Answer: scores on homeworks, projects, labs
- Model performs 95% accuracy on test set
  - Is this a good performance?



- Model performs 95% accuracy on test set
- Is this good performance?
- Depends:
  - If 90% of students passed, 95% accuracy isn't that great, its not much better than just saying everyone passed (this would get us 90% accuracy)
  - If 50% of the students passed, 95% accuracy seems good
- Final Project: make sure to contextualize your model's performance with a majority baseline (always predicting one of the classes)

# Evaluation Metrics



		True Class	
		Positive	Negative
Predicted Class	Positive	TP	FP
	Negative	FN	TN

Image from towardsdatascience



- Accuracy:  $\frac{TP}{TP+FP+FN+TN}$

- Precision:  $\frac{TP}{TP+FP}$

- Recall/Sensitivity:  $\frac{TP}{TP+FN}$



A blue-tinted photograph of a statue, likely a personification of Liberty or Justice, holding a torch aloft in its right hand. The statue is set against a background of trees and a clear sky. The text "Course Review" is overlaid in a large, white, sans-serif font, centered on the image. Two short white horizontal lines are positioned above and below the text.

# Course Review



- Computation: Python and Tables
- Exploration
  - Discover patterns in data
  - Articulate insights (visualizations)
- Inference
  - Make reliable conclusions about the world
  - Probability & Statistics
- Prediction
  - Informed guesses about unseen data
  - Machine Learning: Regression & Classification



- Textbook sections
  - General features and Table methods: 3.1 - 9.3, 17.3
  - `sample_proportions`: 11.1
  - `percentile`: 13.1
  - `np.average`, `np.mean`, `np.std`: 14.1, 14.2
  - `minimize`: 15.4



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# Exploring Data

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- Qualitative:
  - Visualizing Distributions: Chapter 7
  
- Quantitative
  - Center and spread: 14.1-14.3
  - Linear trend and non-linear patterns: 8.1, Chapter 15



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# Inference

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- Study, experiment, treatment, control, confounding, randomization, causation, association: Chapter 2
- Distribution: 7.1, 7.2
- Sampling, probability sample: 10.0
- Probability distribution, empirical distribution, law of averages: Chapter 10
- Population, sample, parameter, statistic, estimate: 10.1, 10.3
- Model: every null and alternative hypothesis; 16.1



- To make conclusions about unknown features of the population or model, based on assumptions of randomness





# Inference: Estimation



- Question: What is the value of the parameter?
- Terms: **predict, estimate, construct a confidence interval, confidence level**
- Answer: Between  $x$  and  $y$ , with 95% confidence
- Method (13.2, 13.3):
  - **Bootstrap the sample**; compute estimate
  - Repeat; draw empirical histogram of estimates
  - Confidence interval is “middle 95%” of estimates
- Can replace 95% by other confidence level (not 100%)

# Meaning of “95% Confidence”



- You'll never get to know whether or not your constructed interval contains the parameter.
- The confidence is in the process that generates the interval.
- The process generates a good interval (one that contains the parameter) about 95% of the time.
- End of 13.2



- To **estimate** a numerical parameter: 13.3
  - Regression **prediction**, if regression model holds:  
Predict  $y$  based on a new  $x$ : 16.3
  
- To **test** whether or not a numerical parameter is equal to a specified value: 13.4
  - In the regression model, used for testing whether the slope of the true line is 0: 16.2



# Inference: Testing



- **Null:** A completely specified chance model, under which you can simulate data.
  - Need to say exactly what is due to chance, and what the hypothesis specifies.
- **Alternative:** The null isn't true
  - something other than chance is going on; might have a direction
- **Test Statistic:** A statistic that helps decide between the two hypotheses, based on its empirical distribution under the null
- 11.3



# Types of Tests



## 1 Sample: One Category (e.g. percent of black male jurors)

- Test Statistic: `empirical_percent`, `abs(empirical_percent - null_percent)`
- How to Simulate: `sample_proportions(n, null_dist)`

## 1 Sample: Multiple Categories (e.g. ethnicity distribution of jury panel)

- Test Statistic: `tvd(empirical_dist, null_dist)`
- How to Simulate: `sample_proportions(n, null_dist)`

## 1 Sample: Numerical Data (e.g. scores in a lab section)

- Test Statistic: `empirical_mean`, `abs(empirical_mean - null_mean)`
- How to Simulate: `population_data.sample(n, with_replacement=False)`

## 2 Samples: Numerical Data (e.g. birth weights of smokers vs. non-smokers)

- Test Statistic: `group_a_mean - group_b_mean`,
  - `group_b_mean - group_a_mean`, `abs(group_a_mean - group_b_mean)`
- How to Simulate: `empirical_data.sample(with_replacement=False)`





- The chance, **under the null hypothesis**, that the test statistic comes out equal to the one in the sample or more in the direction of the alternative
- If this chance is small, then:
  - If the null is true, something very unlikely has happened.
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- Even if the null is true, your random sample might indicate the alternative, just by chance
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**Prediction**  
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- Regression model 16.1
- Bootstrap confidence interval for the true slope 16.2
  - Use of this interval to test if the true slope is 0
- Bootstrap prediction interval for  $y$  at a given value of  $x$  16.3



- Binary classification based on attributes 17.1
  - $k$ -nearest neighbor classifiers
  
- Training and test sets 17.2
  - Why these are needed
  - How to generate them
  
- Implementation: 17.4
  - Distance between two points
  - Class of the majority of the  $k$  nearest neighbors
  
- Accuracy: Proportion of test set correctly classified 17.5



# Data Science



# Jupyter on your own



- Installing Anaconda - <https://www.anaconda.com/products/distribution>
- Open up the Anaconda Navigator
- Launch a new notebook
- Install “datascience” package:
  - `pip install datascience`





- Resources from Brian Mailloux:
  - <https://edblogs.columbia.edu/eescx3050-001-2015-3/category/classes/class-1-intro/>
  - <https://youtu.be/FOJG3PxqWV0>



- Unprecedented access to data means that we can make new discoveries and more informed decisions
- Computation is a powerful ally in data processing, visualization, prediction, and statistical inference
- People can agree on evidence and measurement
- Data and computation are everywhere: understanding and interpreting are more important than ever



- Evidence and measurements are critical ingredients for good decision-making
  - ...but they're not enough by themselves!
- Data science is a powerful complement to qualitative analysis
  - but it's not a replacement!



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- Visualize, then quantify!
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- Table manipulation using Python
- Working with whole distributions, not just means
- Decisions based on sampling: assessing models
- Estimation based on resampling
- Understanding sampling variability
- Prediction



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**Thank you!**  
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# Course Review

(in depth)

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- Median
  - 50th percentile, where
  - $p$ th percentile = smallest value on list that is at least as large as  $p\%$  of the values 13.1
  - Median is not affected by outliers
- Mean/Average
  - Depends on all the values
  - smoothing operation
  - center of gravity of histogram
    - if histogram is skewed, mean is pulled away from median towards the tail



- Standard deviation (SD) measures roughly how far the data are from their average
- $SD = \text{root mean square of deviations from average}$

Steps:    5        4        3                    2                                    1

# Chebyshev's Bounds



Range	Proportion
average $\pm$ 2 SDs	at least $1 - 1/4$ (75%)
average $\pm$ 3 SDs	at least $1 - 1/9$ (88.888...%)
average $\pm$ 4 SDs	at least $1 - 1/16$ (93.75%)
average $\pm$ 5 SDs	at least $1 - 1/25$ (96%)

**True no matter what the distribution looks like**



# Bounds and Normal Approximations



<b>Percent in Range</b>	<b>All Distributions</b>	<b>Normal Distributions</b>
Average +/- 1 SD	At least 0%	About 68%
Average +/- 2 SDs	At least 75%	About 95%
Average +/- 3 SDs	At least 88.888...%	About 99.73%



“average  $\pm$  SDs”

14.2

- z measures “how many SDs above average”
- Almost all standard units are in the range (-5, 5)
- To convert a value to standard units:

$$z = \frac{\text{value} - \text{average}}{\text{SD}}$$



- Measures *linear* association
- Based on standard units; pure number with no units
- $r$  is not affected by changing units of measurement
- $-1 \leq r \leq 1$
- $r = 0$ : No linear association; *uncorrelated*
- $r$  is not affected by switching the horizontal and vertical axes
- Be careful before you use it
- 15.1



## Correlation Coefficient ( $r$ ) =

average of product of standard( $x$ ) and standard( $y$ )

Steps:            4                            3                            2                            1

Measures how clustered the scattered data are around a straight line

**estimate of  $y = r \cdot x$** , when both variables are measured in standard units



*estimate of  $y = \text{slope} * x + \text{intercept}$*

*slope of the regression line*

$$r * \frac{SD \text{ of } y}{SD \text{ of } x}$$

*intercept of the regression line*

$$\text{mean}(y) - \text{slope} \times \text{mean}(x)$$



- Regression line is the “least squares” line
- Minimizes the root mean squared error of prediction, among all possible lines
- No matter what the shape of the scatter plot, there is one best straight line
  - but you shouldn't use it if the scatter isn't linear
- 15.3, 15.4



- Error in regression estimate
- One residual corresponding to each point  $(x, y)$
- **residual**
  - = **observed  $y$  - regression estimate of  $y$**
  - = vertical difference between point and line
- No matter what the shape of the scatter plot:
  - Residual plot does not show a trend
  - Average of residuals = 0



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- Probability theory:
  - Exact calculations
  - Normal approximation for mean of large random sample
  - Accuracy and sample size

# Equally Likely Outcomes



**Assuming** all outcomes are equally likely, the chance of an event  $A$  is:

$$P(A) = \frac{\textit{number of outcomes that make } A \textit{ happen}}{\textit{total number of outcomes}}$$



## Central Limit Theorem

If the sample is

- large, and
- drawn at random with replacement,

Then, *regardless of the distribution of the population,*

**the probability distribution of the sample sum (or of the sample mean) is *roughly* bell-shaped**



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- **Null:** The sample was drawn at random from a specified distribution.
- **Test statistic:** Either count/proportion in one category, or distance between count/proportion and what you'd expect under the null; depends on alternative
- **Method:**
  - **Simulation:** Generate samples from the distribution specified in the null.
- 11.1 (Swain v. Alabama, Mendel)



- **Null:** The sample was drawn at random from a specified distribution.
- Test statistic: TVD between distribution in sample and distribution specified in the null.
- Method:
  - Simulation: Generate samples from the distribution specified in the null.
- 1.2 (Alameda county juries)



- **Null:** The two samples come from the same underlying distribution in the population.
- Test statistic: difference between sample means (take absolute value depending on alternative)
- **Method for A/B Testing:**
  - Permutation under the null: 12.2 (Deftategate), 12.1 (birth weight etc for smokers/nonsmokers), 12.3 (BTA randomized controlled trial)





- **Null:** parameter = a specified value.
- **Alternative:** parameter  $\neq$  value
- **Test Statistic:** Statistic that estimates the parameter
- **Method:**
  - **Bootstrap:** Construct a confidence interval and see if the specified value is in the interval.
- 13.4, 16.2 (slope of true line)



- Tests of hypotheses can help decide that a difference is not due to chance
- But they don't say *why* there is a difference ...
- Unless the data are from an RCT 12.3
  - In that case a difference that's not due to chance can be ascribed to the treatment



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